Question 2

# Question a) Is there a relationship between tea temperature and area of residence?

Here is the given table:

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Area of residence | Temperature | | | | Total |
| < 60 | 60-64 | 65-69 | >= 70 |
| Urban | 4200 | 3646 | 1566 | 537 | 9949 |
| Rural | 14758 | 15260 | 6490 | 2125 | 38633 |
| Total | 18958 | 18906 | 8056 | 2662 | 48582 |

**Formulate an appropriate null and alternative hypotheses:**

H0: tea temperature and area of residence are independent. (The representation of each tea temperature is the same whether the area of residence is urban or rural)

HA: tea temperature and area of residence are not independent. (The representation of each tea temperature is different, depending on whether the area of residence is urban or rural)

**Hypothesis test:**

If H0 were true, we would expect the number of people in each category to be:

We can fill out the table with expected values:

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Area of residence | Temperature | | | | Total |
| < 60 | 60-64 | 65-69 | >= 70 |
| Urban | 3882.367 | 3871.718 | 1649.77 | 545.1451 | 9949 |
| Rural | 15075.63 | 15034.28 | 6406.23 | 2116.855 | 38633 |
| Total | 18958 | 18906 | 8056 | 2662 | 48582 |

Now that we have the expected values and the given values in two tables, we can compare them to calculate **the chi-square test statistic:**

**P-value:**

Using software, we can discover: p-value < 0.00001

**Output from R:**

Pearson's Chi-squared test

data: teaData

X-squared = 54.729, df = 3, p-value = 7.843e-12

**Conclusion:**

With a p-value so small, there is evidence against the null hypothesis, and therefore evidence for the alternative hypothesis, regardless of any reasonable alpha value. In the context of this problem, this means that tea temperature and area of residence are not independent. In other words knowing the area of residence for a data set will give hints about the expected distribution of tea temperature consumed for that data set, and vice versa.